

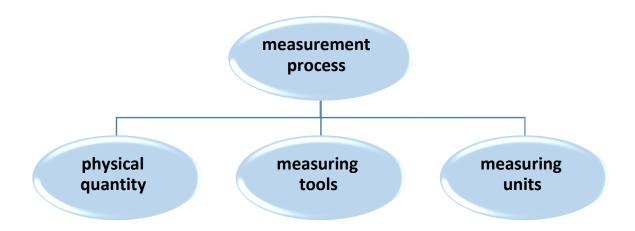
**Egyptian pioneer School- languages** 

Physics First secondary 2023 -2024

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#### **Physical measurements**

\*measurement process:it's the process of comparing an unknowing quantity with another known quantity of it's kind to find out how many times the first includes the second



## 1) Types of physical quantities

<b>Fundamentalphysical quantities</b>	<b>Derived physical quantities</b>
they are physical quantities that	they are physical quantities that
cannot be defined in terms of other	cannot be defined in terms of the
physical quantities	fundamental physical quantities
Ex:length-mass-time	Volume-speed-acceleration

## 2)Tools of measurement

Ancient:length--->arm,hand,food

Time--->sunrise,sunset and moon phases

#### recently

## length

1-meter tape ->suitable for lengths such as dimensions



of room

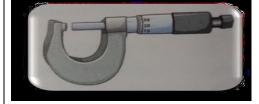
vernier caliper->suitable for small lengths such as the diameter of pen



2-Ruler->suitable for lengths such as length of book



3-Micrometer->suitable for very small lengths such as thickness of apaper



#### mass

1-roman balance: it is used in ancient times but it has alarge percentage of error



2-Two pan balance It measureing in kilogram



3-One pan balance: measuringin kilogram such as measuring the mass of fruits



4-Digital balance:measuring very small masses such as golden accessories



#### time

1-hour glass->oldest tool todetermine time



2-Stop watch>measure a
certain interval of
time



3-Pendulum Clock>depend on energy conservation law



4-Digital watch->newest tool used in our daily life



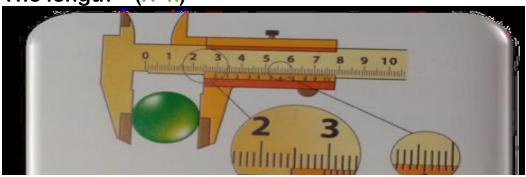
## How to use vernier ??

1)measure the reading of fixed scale (X) 1mm; use zero of sliding scale (Where the number that facing zero is the reading)

2)measure the reading of sliding scale (x) 0.9mm; use fixed scale (the line on sliding scale lines up to fixed scale)

\*Note that the reading of sliding scale( \* 0.1)

The length = (X+x)



The reading of

this vernier: (X) = 2.9 cm = 29 mm, (x) = 6 \* 0.1 = 0.6 mm

The diameter of vernier = (X+x) = 29+0.6 = 29.6 mm

## 3)Measuring units

## A physical quantity without its unit is meaningless

	The french system (C.G.S)	The british system (F.P.S)	The metric system (M.K.S)
Length(I)	Centimeter(cm)	Foot(ft)	Meter(m)
Mass(m)	Gram(g)	Pound(lp)	Kilogram(kg)
Time(t)	Second(s)	Second(s)	Second(s)

## \*international system of units(SI units)

The physical quantity	The international units
1-Length(I)	Meter(m)
2-Mass(m)	Kilogram(kg)

3-Time (t)	Second(s)
4-Electric current intensity(I)	Ampere(A)
5-The absolute temperature(T)	Kelvin(K)
6-Amount of material(n)	Mole(mol)
7-Luminous intensity(I <sub>v</sub> )	Candela(cd)
8-Angle measure	Radian(rad)
9-Solid Angle measure	Steradian(sr)
-	

#### Standard(length)meter

# It's the distance between two engraved marks at the ends of a rod made of platinum and iridium alloy kept at 0°C

The standard time (second)

in encient: use day and night time

Solar day 24 hour, hour =60 min, min = 60 sec

The second =1\86400of the average solar day

Now: atomic clocks (cesium clock)

## cesium clock used for:

1) determining the duration of the earth spin .

2) checking up for aviation and navigation.

3) verifing the journey schedule of space ships that explore the universe



## The standard mass(kilogram)

# It is the mass of culinder made of platinum and iridium alloy of specific dimentions kept at0<sup>0</sup>C

## \*give reason for:

# <u>Platinum and iridium alloy used in standard unit instead of other materials such as glass?</u>

Because 1-it is a rigid 2-chemically inactive 3-not affected by surrounding temperature contrary to other materials

## **Multiplies and fractions of units**

multiply

 $100000000000 = 1*10^{10}$ 

fraction

 $0.000000001=10^{-10}$ 

## **prefixes**

prefix			micro		•		_	_		
factor	×10 <sup>-</sup>	×10 <sup>-</sup>	×10 <sup>-6</sup>	×10 <sup>-9</sup>	×10 <sup>-</sup>	×10 <sup>12</sup>	×10 <sup>9</sup>	×10 <sup>6</sup>	×10 <sup>3</sup>	×10 <sup>2</sup>
Symbol	С	m	М	n	р	Т	G	M	k	Н

Liter (L)	10-3 <i>m</i> 3=1 <i>cm</i> 3
Angstrom(Å)	10-10 <i>m</i>
Gram(gm)	10–3 $kg$
Ton(ton)	103kg
Femto (fs)	10-15 sec

## The steps of conservation of units:

(1) if unit aren't raised to a power:

Convert the quantity to it's international unit then to the required unit (2) if a units are raised to a power:

Convert the quantity to it's international unit by raising the conversion coefficient to the same power then to the required unit Of unit then convert it to the required unit by raising the conversion coefficient to the same power

Of unit

(3) if units consist of more than one measuring unit:

Convert the numerator and denomiator to the required unit by previous steps

## \*example:

(1)A car moves a distance of 5km, so this distance is equivalent to.....

(b)
$$5x10^{-2}$$
 cm (c) $5x10^{2}$ cm

$$(c)5x10^{2}cm$$

soluation

$$s=5x10^3 \text{ m}$$

$$=5x10^3x10^2cm$$

$$=5x10^{5}$$
cm

(2) there is an electric current of intensity 7 milliampere (7mA), then this ntensity in microampere (µA)is......

 $(a)7x10^3$ 

$$(b)7x10^6$$

$$(c)7x10^{9}$$

(b)
$$7x10^6$$
 (c) $7x10^9$  (d) $7x10^{12}$ 

Solution

$$I=7mA=7x10^{-3}A$$

$$=7x10^{-3}x10^{6}\mu A$$

$$=7x10^{3} \mu A$$

(3)a car moving on a highway at a velocity of 37.5 m/s.if the maximum speed allowed on this road is 120km/h, had the driver exceeded this velocity? (a) yes, the velocity of the car is larger than the allowed velocity by 10km/h

(b) yes, the velocity of the car is larger than the allowed velocity by 15k/h

(c) no, the velocity of the car is smaller than the allowed velocity by 10km/h

(d) no, the velocity of the car is smaller than the allowed velocity by15km/h Solution

V=37.5m/s=37.5
$$\frac{m}{s}$$
=37.5 $\frac{10}{\frac{1}{60}x\frac{1}{60}}\frac{km}{h}$  = 135 $\frac{km}{h}$ 

The driver exceeds the allowed velocity by ( $\Delta v$ ):

The measuring unit of velocity km/h can be converted to m/s as follows : 
$$\frac{5}{18} \times \frac{18}{5}$$

## Dimentional formula

The general dimentional formula of any physical quantity is:

[A]=
$$M\pm^a L\pm^b T\pm^c$$

## How to deduce the dimensional formula of the velocity (v) as an example:

	Steps examples				
1	Write down the mathematical lation that determine the physical quantity	potential energy P.E.=( m.g.h)			
2	Write down the relation in terms of the fundamental	[P.E.]= M. <sup>L</sup> / <sub>t2</sub> .L			
2	(physical quantities) M,L and T Put on each of the symbols M,L and T it's suitable power and arrange them in the order	[F.C.]- IVI. $\overline{t2}$ .L			
3	of) M.L.T(				
	If one or more quantities is not present in the formula it can be				

expressed as  $\mathbf{M}^0 \cdot \mathbf{T}^0$ Such as  $x^0 = \mathbf{1}$  so it's not written. The measuring unit can be obtained from the dimensional formula.

 $M.L^2.T^{-2}$ And it's unit = $Kg.m^2sec^{-2}$ 

Quantity	Rule	D.F	Unit
length		L	m
mass		M	kg
time		Т	S
Area(A)	Length× length	$L\times L=L^2$	$M^2$
Volume(V)	Length × length ×	$L\times L\times L=L^3$	m <sup>3</sup>
	length		
Density(ρ)	mass	$M/L^3=ML^{-3}$	Kg.m <sup>-3</sup>
	Volume		
Velocity(v)	Displacement	LT <sup>-1</sup>	m.s <sup>-1</sup>
	Time		
Accleration(a)	Change of velocity	LT <sup>-2</sup>	m.s <sup>-2</sup>
	Time		
Force(F)	mass×accelration	MLT	Kg.m.S
Work(W)	force ×displacement	ML <sup>2</sup> T <sup>-2</sup>	Kg.m <sup>2</sup> .s <sup>-</sup>
Momentum(P <sub>L</sub> )	mass×velocity	MLT <sup>-1</sup>	Kg.m.s <sup>-1</sup>

**Note:** we can multiply or divide physical quantities of different dimensional formula but it can't be added or subtracted because D.f is M. L. T only without writing anynumerical constants as shown:

- $\bullet \quad \mathsf{M}^*\mathsf{L}\mathbf{T}^{-2} = \mathsf{M}\mathsf{L}\mathbf{T}^{-2}$
- $MLT^{-2} \div M = LT^{-2}$
- $LT^{-2} + LT^{-2} = LT^{-2} \neq 2 LT^{-2}$
- $LT^{-2} LT^{-2} \neq 0 = LT^{-2}$

**Note:** numerical constant such as  $(2, \frac{1}{2}, \pi)$  and

trigonometric functions such as ( $\sin \theta$ ,  $\cos \theta$ ,  $\tan \theta$ ) have no dimensions.

## \*the importance of dimenstional formula:

Verify the validity of a physical relation
\*If X=Y this relation may be correct if the dimensional formula
of (X)=if the dimensional formula of(Y)

Example (1) a body of masss m moves with velocity v and it's kinetic energy is KE, so which of the following relations may be correct? (knowing that:(KE)=ML<sup>2</sup>T<sup>-2</sup>)

$$(a)KE=1/2m^2v$$

$$(c)KE=1/2mv^2$$

$$(d)KE=2m^2v^2$$

(soluation)

\*\*The dimensions of the L.H.S(KE)=ML<sup>2</sup>T<sup>-2</sup>

so the dimensions of the R.H.s must equal ML<sup>2</sup>T<sup>-2</sup>

(2) If measuring unit of a physical is  $Kg/m^2$ .  $s^2$  Then the dimensional formula is ...........

a) $ML^2T^{-2}$  b)  $ML^2T^2$  c)  $ML^{-2}T^{-2}$  d) MLT

- (3): If (x = yz) where the dimensions of
- (x)=  $ML^2T^{-3}$  and the dimensions of (y)=  $LT^{-2}$  then the dimensions of (z) are .....
- a)  $MLT^{-1}$  b) MLT C)  $LT^{-1}$  d)  $MLT^{-5}$

## Work sheet

## Choose the correct answer:

1) the fundamental physical quantities of the following are

- a)length and area
- b) the velocity and the acceleration
- c)the mass and volume
- d)the time and the mass
- 2)a common feature in the french system (gaussian), the britich system and the metric system is that they all measure

- a)length b)mass c)time
- d)temperature
- 3)femtosecond =..... microsecond
- a)  $10^{-15}$
- **b)**  $10^{-9}$  **c)**  $10^9$
- **d)** 10<sup>6</sup>
- 4) if x=10g and y=10 kg, then the value of (x+y) is

- a)10.1 kg
- b)100.1 g c)10.01 kg
- d)10.01 g
- 5)how many bottles of volume 10000  $cm^3$  is enough to fill a tank of capacity 1  $m^3$
- a)1
- b)
- 10
- c)1000
- d)100
- 6) if the measuring unit of acceleration is  $m/s^2$  and its dimensional formula is Lx.T-v
- a)x=1, y=1

- b)x=1, y=2 c)x=1, y=-2 d)x=-1,y=2
- 7)if the dimension formula of the quantity A are M.L2.T-2 and the dimensions of the quantity B are M.L2.T-2, then the quantity of (2B-A) .....
- a)has dimensional formula  $M.L2.T^{-2}$
- b)has dimensional formula  $M2.L4.T^{-4}$
- c)has dimensional formula  $M3.L6.T^{-6}$
- d)isn't a physical quantity

8)th measuring unit of the physical dimensional formula of $M.L.T^{-1}$	•
	is equivalent to $Kg.m/s^2$ , the joule
<b>a)</b> $N.m$ <b>b)</b> $J.m^{-1}$ <b>d)</b> $J.s^{-1}$	c)N.s
of radius r that moves at veloc	e liquid resists the motion of a ball ity v is given by the relation F=krv of the quantity k is
a) $M.L.T$ b) $M^{-1}.L.T$ c	$)M^{-1}.L^{-1}.T$ <b>d</b> $)M.L^{-1}.T^{-1}$
10)a body of initial velocity $vist$ acceleration (a) to cover a displacement(d) velocity $v_f$ after this time *which of the following equation:	within time (t) to reach final
• •	$)v_f^2 = v_i^2 + 2ad$ $)v_f = v_i + at$
or derived quantity? and why	a measured by $kg.m^{-3}$ fundamenta?
2)deduce the dimensional form 1) Force(F) 2) Work (W) 3) p ( P= F/A)	•

	••
	••
)why is not the glass used in manufacturing of the standard neter?	
	• • •

## Lesson(2)types of measurement&measurement error

Measurement process cannot be accurately 100% but there should be even a simple percentage of error.

## Reasons for measurement errors:

No.	Reason	Example	Figure
1	Choosing unsuitable tool	Using a normal balance instead of sensitive balance to measure mass of a golden ring.	Some of the state
2	A defect in the measuring tool	Old ammeter, Due to weak magnet and pointer of ammeter does not start from zero graduation.	A CLASS 2.5
3	Wrong procedure	The vision must be perpendicular to the cylinder.	19.82 ml 19.70 ml 19.62 ml
4	Environmental factors (temperature, humidity and air currents)	Using sensitive balance in presence air currents.	in connect in

Average of reading =  $\frac{sum\ of\ reading}{the\ number\ of\ taking\ reading\ for\ the\ measured\ quantity}$ 

<sup>\*</sup>note :to reduce the error precentage in the measurement we calculate the average as follows:

Types of measurement

<u>Direct measurement</u>	<u>indirect</u> measurement	
One measuring tool is used	More than one measuring tool is used	
No mathematical relation is	A mathematical relation is applied to	
applied	find the quantity	
One measurement error may	More thanOne measurement error may	
<u>occur</u>	<u>occur</u>	
Like measure the density by	Like measure the density by measure	
using the hydrometer	mass and volume	
READ AT BOTTOM OF MENISCUS READING: 22.5	measuring cylinder 20 cm <sup>3</sup> water electronic balance	

## 1- Calculation of error in direct measurement

Absolute error $(\Delta x)$	Relative error (r)
The difference between actual value for measuring quantity $(x_0)$ and measured value $(x)$ $\Delta x =  x_0 - x $	The ratio between absolute error $(\Delta x)$ to real value for measuring quantity $(x_0)$ $\mathbf{r} = \frac{\Delta x}{x_0}$
This sign of modulus (   ) indicates the results are (+ve) even if the real value less than measuring quantity.	The relative error indicates accuracy of measurement as long as relative error decreases the measurement is more accurate.

## Has measuring unit

Which is the same as the unit of the physical quantity.

# Has no measuring unit Because it's the ratio between two quantitieshaving the same measuringunit.

• The result of measurement is expressed as  $(x_o \pm \Delta x)$ .

$$\Delta x = |x - o - x|$$

#### relative error

$$r = \frac{\Delta x}{x_o}$$

## example:

**Example** 1: student measures length of pencil = 9.9 cm and real length of it = 10cm while another student measures length of room = 9.13m while real length of it = 9.11m.

- a) Calculate the absolute error and the relative error in each case.
- b) In which case was the measurement more accurate andwhy.

## **Solution:**

## In case the first student

• the absolute error

## In case the second student

• the absolute error

$$\Delta x = |x_0 - x| = |10 - 9.9|$$
  
= 0.1 cm

the relative error

$$\mathbf{r} = \frac{\Delta x}{x_0} = \frac{0.1}{10} = 0.01 = 1\%$$

The length of pencil

$$= (10 \pm 0.1)$$
 cm

$$\Delta x = |x_0 - x| = |9.11 - 9.13|$$
  
= 0.02 m = 2 cm

• the relative error

$$r = \frac{\Delta x}{x_o} = \frac{0.1}{10} = 0.01 = 1\%$$
  $r = \frac{\Delta x}{x_o} = \frac{0.02}{9.11} = 0.0022 = 0.22\%$ 

The length of room

$$= (9.11 \pm 0.02) \,\mathrm{m}$$

b) The measurement in the second case is more accurate because the relative error in second case is less than that in the first case.

## 2- Calculation of error in indirect measurement

	T	I
Mathematical relation	Example	How do you calculate the error?
Addition	Measure volume of two amount of liquid $V_T = V_1 + V_2$	Absolute error $(\Delta x)$ = absolute error in the first measurement +
Subtraction	Measure volume of coin = (volume water +coin)( $V_2$ ) - volume of water( $V_1$ ) $V_{coin} = V_2 - V_1$	absolute error in the second measurement $\Delta x = \Delta x_1 + \Delta x_2$ The relative error (r) = $\frac{\Delta x}{x_0}$
Multiplication	Measure area of rectangle by measuring the length and the width then multiple (length × width).	The total relative error (r) = the relative error in the first measurement + therelative error in
Division	Measure density of liquid $D = \frac{M}{v} = \frac{mass}{volume}$	the second measurement $r_T$ = $r_1$ + $r_2$ the absolute error $\Delta x$ = $r_T$ . $x_o$

**Example**: In an experiment for determination of physical quantity (L) that is formed from ,  $L_2$  Where  $L_1$  = (5.2 ± 0.1) cm and  $L_2$  = (5.8 ± 0.2) cm. Calculate value (L) and the relative error.

#### **Solution:**

The real value 
$$(L_o)$$
 = 5.2 + 5.8 = 11 cm

Absolute error (
$$\Delta L$$
)= 0.1+0.2 = 0.3 cmL

= 
$$L_o \pm \Delta L$$
 = (11 ± 0.3) cm

Relative error(r)=
$$\frac{\Delta L}{L_0}$$
= $\frac{0.3}{11}$ == .027

#### Work sheet

#### Choose the correct answer:

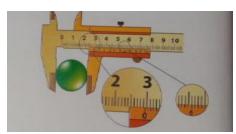
1) the best way to judge the accuracy of measurement is though

- a)absolute error
- b) dividing of the relative and absolute error
- c)the product of the relative and absolute error
- d) relative error

2) the relative error in measuring the area of a room is 0.06 where the actual value of the area is  $30m^2$ , then the absolute error in measuring this area is.....

- a)1.8 $m^2$
- **b)0.002** $m^2$  **c)0.06**  $m^2$  **d)1.2**  $m^2$

3) the vernier caliper was used to measure the diameter of a metallic



ball as shown, then:

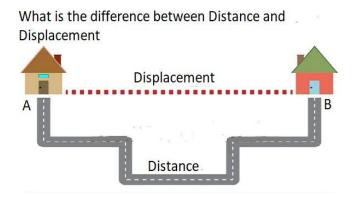
\*the measured value =.....

b)2.45 cm c)2.46 cm d)2.64 cm a)2.54 cm

				)
a)4.3% , 0.11 cm c)2.8% , 0,11 cm				b)0.4% , 0,01 cm d)3.2% , 0.01 cm
•	_		_	the side length of a suring its volume is
a)0.01	b)0.02	c)0.03	d)0.04	
and the rela	tive error f	for each d a	nd t is 0.2	ed by equation $v{=}\Delta d\Delta t$ 2 ,0.1 and absolute velocity
a)0.45	b)0.2	c)15		d)5
essay quest	ions:			
•				or masurement ous sentence .
			••••••	••••••
				•••••
2)there are 4 different physical quantities and their results were a) $(10\pm0.1)$ b) $(1\pm0.01)m$ c) $(50\pm0.5)kg$ d) $(200\pm0.02)s$ arrange these measurements in ascending order according to their accuracy .				

## **Chapter(2)**Scalar Quantity Vector Quantity

chapter(2) scalar quarter	ty rector quartery
Scalar quantity	Vector quantity
It is a physical quantity that can	It is a physical quantity that can
be	be
fully defined by its magnitude	fully defined by both magnitude
only,	and direction.
it has no direction.	
Examples☺	Examples <sup>©</sup>
1 - Distance.	1 - Distance.
2 - Speed.	2 - Speed.
3 - Time.	3 - Time.
4 - Mass.	4 - Mass.
5 - Energy.	5 - Energy.
6 - Temperature.	6 - Temperature.
<u>Distance(s)</u>	<u>Displacement(d)</u>
The length of the path from start	The length of straight line from
point to end point	start point to end point and the
Scalar quantity	<u>direction (shorter distance)</u>
Always positive	Vector quantity
	It may be positive ,negatgive or
	<u>zero</u>



\*The magnitude of the displacement is less than or equal the covered distance \*If the body moves from position  $x_i$ to position  $x_f$  the displacement calculated from the relation  $d=x_f-x_i$ 

In one direction	constant	From a to b , then the magnitude of displacement = the distance	A Distance  Displacement  B
In 2 directions	opposite	*doesn't return to its starting point : distance = ab +bc Displacement = ab- bc (Note )*return to the starting point : Distance = 2ab Displacement = 0	A B C B Displacement

## If body moves in 2 dimensions:-

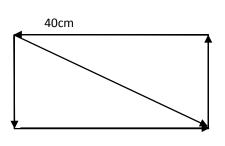
	.3 III 2 diffictions	
In straight	Distance =AB+BC	АВ
path	Displacement=AC	
	Distance =AB+BC+CD	Î B
	Displacement=AD	D C B
	Distance = AB+BC+CD+DA	t c
	Displacement=0	
In curved	Distance Quate	Quarter revolution
path	=12 $\pi r$ revolution	г
	Displacement	A
	=V2 <i>r</i>	Half revolution
		A B
	Distance = $\pi r$	Complete revolution
	Displacement=2 <i>r</i>	A
	Distance = $2\pi r$	r
	Displacement=0	

## **Example**:

In the rectangle in the fig Calculate the distance and displacement in



b



BB, AC, AD, along perimeter of rectangle

Solution:

Displacement = 
$$\sqrt{30^2 + 40^2} = 50 \text{ m}$$

Along perimeter of rectangle:

## **Representation of vector quantities**

## the vector quantity is represented by a directed straight

segment( )whose base is at the starting point and its tip is at the end point :

## \*some basics of vector algebra:-

1)two vectors are equal if( $A^{\rightarrow}$ = $B$ )	2) two vectors are not equal if $(A^{\rightarrow} \neq B)$	3)negative vectors	4)the product of a constant magnitude by a vector
	Have different directions (even if they have thesamemagnitude) *differenet magnitudes (even if they have the same direction)	magnitude of possitve vector but has the opposite	, ,

<sup>\*</sup>its length is proportional to the vector magnitude

<sup>\*</sup>the arrow direction points to the direction of the vector quantity

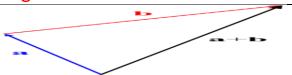
<sup>\*</sup>the vector quantity is denoted by a bold letter(A)or a letter tagged by a small arrow which always refers to the right side ( $\rightarrow$ )

## **Vector algebra**

## 1) addation and subtraction:

#### We have two methods:-

## 1)triangle method



If the end of the first vector is the start of thesecond one.

Draw a triangle as shown in Figure and the resultant vector representative by the vector starting from start point of first vector to the end point of the second vector

## 2rectangle method

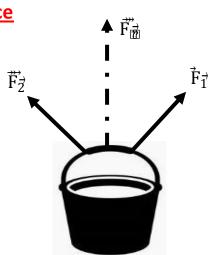


If they have the same startpoint

Draw a parallelogram where A and B are two adjacent sides and the resultant vector representative by the diameter as shown in Figure have the same start point

## **Resultant force**

When two forces or more act on an object (as shown in fig)it will move in a certain direction determined by the resultant of the forces acts on the object which is called **Resultant force**( $\vec{F}_{\vec{R}}$ )



The Resultant force  $(\vec{F}_{\vec{R}})$  is a single force that produce the same effect on an object as that produced by the original acting forces.

## Resolution of the vector

<u>To determine the net (Resultant) force of two perpendicular forces:</u>

\*To measure the value of an **angle** 
$$(\theta)$$
 by the relations:

Sin 
$$\theta = \frac{Opposite}{Hypotenuse} = \frac{\overline{B}}{A}$$

$$\cos \theta = \frac{Adjacent}{Hypotenuse} = \frac{R}{A}$$

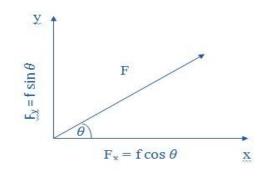
Tan 
$$\theta = \frac{Opposite}{adjacent} = \frac{B}{AB}$$

## **Analysis of the vector:**

The force can be resolved into:

$$F_x = F \cos(\theta)$$

$$F_y = F \sin(\theta)$$

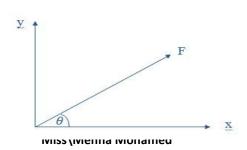


**Example**: a boy pulls a stone with a force (20N) by a string makes angle (30°) with the ground. Calculate the force's value in x-direction and y-direction.

#### Solution:

$$F_x = F\cos(\theta) = 20\cos 30 = 17.3 \text{ N}$$

$$F_v = F \sin(\theta) = 20 \sin 30 = 10N$$

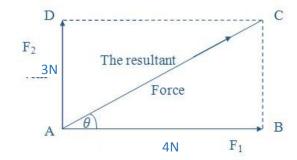


**Example 4**: If a force of (4N) acts on an object on x-axis direction and another force (3N) acts on the same object in Y-axis direction. Find the **resultant force** on this body.

#### Solution:

$$F^2 = F_x^2 + F_y^2$$

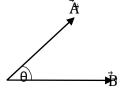
$$F = \sqrt{F_x^2 + F_x^2} = \sqrt{3^2 + 4^2}$$



Tan 
$$\theta = \frac{Opposite}{adjacent}$$

 $\theta = 36.87^{\circ}$  ......(direction)

2) Multiplication of vectors (There are two types):



## 1) Scalar product (Dot Product):

$$\overrightarrow{P} \cdot \overrightarrow{\mathbb{B}} = | 2 | B | \cos(\theta)$$
 (scalar quantity)

If 
$$\theta=90^{\circ}$$
 Then  $(\overrightarrow{A} \cdot \overrightarrow{B}) = |A| |B| \cos(90) =$ 

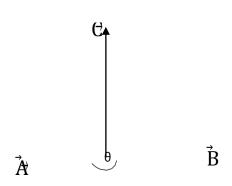
zero

If  $\theta=0^{\circ}$  Then  $((\vec{C},\vec{B})) = |A| |B| \cos(0) = (\text{maximum value})$ 

## 2) Vector product (cross Product):

When multiplying to vectors  $\vec{A}$  and  $\vec{B}$  the result will be another vector  $\vec{C}$  which is perpendicular to the plan of both vectors  $\vec{A}$  and  $\vec{B}$ .

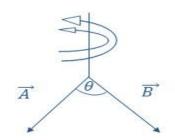
The vector (cross) product of two vectors  $\vec{A}$  and  $\vec{B}$  is expressed as:



$$\mathbf{C} = \mathbf{A} \wedge \mathbf{B} = |\mathbf{A}| |\mathbf{B}| \sin(\mathbf{\Theta}) \mathbf{n}$$

## Right hand rule

 $\vec{n}$ : is the unit vector perpendicular to the plane of  $\vec{A}$  and  $\vec{B}$ .



$$|\vec{A}| \wedge \vec{B} = |A| |B| \sin(\theta) \vec{n}$$
 (Vector quantity)

If  $\theta = 90^{\circ}$  Then  $\vec{B} = |A| |B| \sin (90) \vec{n} = (\text{maximum value})$ 

If 
$$\theta=0^{\circ}$$
 Then  $\vec{A} \cdot \vec{B} = |A| |B| \sin(0) \vec{n} =$  zero

Notes: right hand rule is to determine the direction of  $oldsymbol{c}$ 

If  $\vec{A} \land \vec{B} (\vec{A} t \circ \vec{B})$  the vector  $\vec{C}$  will be upward and vice versa

$\vec{A}$ $\vec{B} = \vec{B} \vec{A}$	$ \vec{A} \times \vec{B}  =  \vec{A} \times \vec{B} $ if $\theta = 45^{\circ}$
$\vec{A} \wedge \vec{B} \neq \vec{B} \wedge \vec{A}$	$\vec{A} \wedge \vec{B} = - \vec{B} \wedge \vec{A}$
$\vec{A} \wedge \vec{B} = 0 \text{ if } \theta = 0^{\circ} (\vec{A} / \vec{B})$	$\vec{A}$ . $\vec{B}$ =0 if $\theta$ =90° ( $\vec{A}$ $\perp$ $\vec{B}$ )

## work shEET

*Choose the co	orrect answer:	• •			
1)a rubber ball	fell from 50 cr	n high and	d kept	boncing alo	ng a vertical path
to reach 30 cm	then 10 cm *t	he total d	listance	e covered by	the ball is
•••••					
a)180 cm	b)130 cm	c)129 c	m	d)90 cm	
2)two forces ac	ct on the same	body, on	e of th	em F1 is in	the direction of
north and its m	nagnitude is 9 I	N and the	other.	F2 in the dir	ection of west
_	ude is 12 N , th	en the ma	agnitud	le of the res	ultant of the two
forces F					
equals					
a)225 N	b)12√2N	c)15 N	d)√1	L5 N	
2) :		l£	1.		
3) in right hand					
ajtirst	vector			c)scala	ar product
4) an athlata an	مرامع مانمهام	d)vector	-		40t. 1400 no to
•					returned 100 m to
the west the di				•••••	
a)350 m b)25	50 III - C)150 I	ii uji	00 111		
and the displac	rement of this	athlete			
a)350 m to eas				m to east	d)150 m to west
4,550 III to cus	. 5,550 m c	o west	0,130	m to cast	a, 150 m to west
6)an object has	moved from	oosition A	to pos	sition B cove	rs 6 m then it
changes its dire	•		•		
J		•			A B
					C
*the covered d	· •				
*the displacem	•	•			
a)14 m in AC di		b)14 m in			
c)10 m in AC di	rection	d)10 m in	CA dir	ection	

7)an object moves along the circumference of a circle of radius r . the ratio between the distance covered by it and the magnitude of its displacement during ½ of a revolution is				
a) $\pi$	b) $2\pi$		c)π/2	$d)\pi/4$
-	gnitude of t			has magnitude 4 units, ors $A$ and $B$ can not

# Unit (2):linear motion Lesson (1): Motion and velocity

Objects around us can be sorted into stationary objects and moving objects. As we study the motion of different objects, it is necessary to describe and understand such motion. The vague ideas about motion convert travelling by ships, trains and planes into a mess. Schedules of departure and arrival of different transportations are mainly based on distances, times and speeds. So, in this chapter we are going to investigate the concept of motion and the related physical quantities

1)Motion : the change in position of an object relative to another static object as time passes .

## \*Types of motion:-

Translational motion	Periodic motion
The motion which has starting	The motion that repeats itself
point	in
Andend point	.equal interval of time
.Motion in straight line	.Motion in circle

## 2) Velocity

the rate of change of displacement.

Or: the displacement of an object in one second.

. It ismeasured in (m/s) or (km/h).

Velocity = 
$$\frac{\text{the change of displacement}}{\text{Time of change}} = \boxed{22 \frac{22}{\Delta t}} = v = \frac{d_2 - d_1}{t_2 - t_1}$$

Example 1: Using the following motion diagram for athlete

displacements every one second. Calculate the velocity of him.

**Solution:** We can describe the motion of athlete using the following table



Time(s)	0	1	2	3	4	5	6
Displacement(m)	0	5	10	15	20	25	30

Velocity = the change of displacement
Time of change

\_\_\_\_\_

## Types of velocity:

## (A) Speed and Velocity:

Focusing on the speedometer of a car, its pointer swings right and left during car movement. The pointer reading specifies the value of the car speed (for example, 80 km/h) without defining the direction of the car motion. This value is known as (Speed).



However, just saying that a car moves at 80 km/h is an incomplete description since no hint is given about the direction of the car motion. Accordingly we need to define such direction to give a full description for the car motion. For instance, saying that the car moves at 80 km/h to east. In this case, we call this (Velocity).

Point of comparison	Speed	Velocity
Definition	The distance moved by an object by unit time	The displacement of an object by unit time
The Type	Scalar quantity	Vector quantity
The Sign	Always positive $v = \frac{change\ of\ istance}{change\ of\ time}$	Can be positive or negative depend on the direction of motion

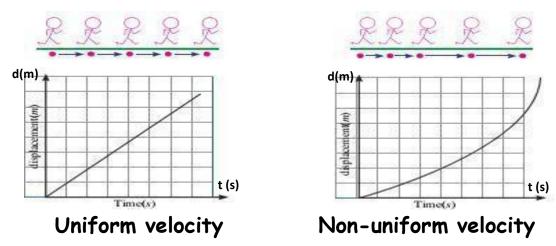
Note: (speed = velocity) at straight line motion in one direction.

## B) Uniform and non-uniform Velocity:

As an athlete runs at uniform velocity, his **displacements are equal** in **equal times**. But if he moves at non uniform velocity, his **displacements are unequal in equal times**.

- 1- <u>Uniform velocity:</u> An athlete velocity when it is displaced through equal displacements in equal times. Both the velocity magnitude and direction are constant (when the object moves in a straight line).
- 2- Non-uniform velocity: An athlete velocity when it is displaced through unequal displacements in equal times. Its velocity may change in magnitude or direction.

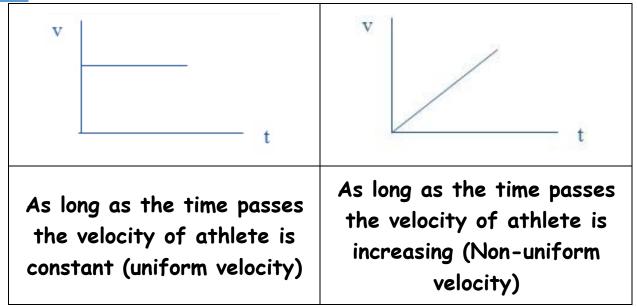
## And it represents graphically as following:



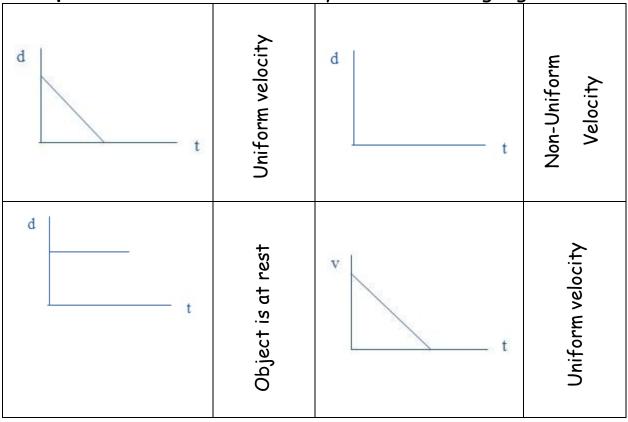
**Uniform velocity:** Represents as **a straight line** due to theequal displacement in equal intervals of time.

**Non-Uniform velocity:** Represents as **a curve** due to theunequal displacement in equal intervals of time.

When plotting the relation between velocity and time wemay get:



Example 2: describe the velocity in the following figures



## C) Instantaneous velocity (v) and average velocity (v)

instantaneous velocity $(v)$	average velocity (*)
The velocity of the object at	The average of the body's
certain instant	velocity during a certain
	interval of time
d Instanteaus velocity	d d t
-v Change in displacement change in time	total displacement total time
$v = \frac{\Delta d}{\Delta t}$	$-v = \frac{d_1 + d_2 + d_3}{t_1 + t_2 + t_3}$

Note: The average velocity differs from the average speed total ditance (scalar quantity)

(scalar quantity). where: average speed =

total time

total displacement But average velocity = total time

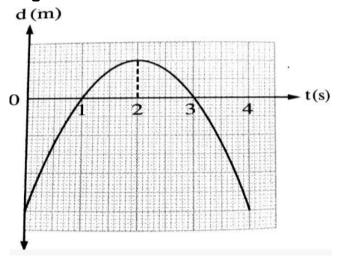
## **Work sheet**

## **Choose the correct answer:**

	ving in a straigh speed		distance of 30	0 m in a minute , the
a)300m/s	b)260 m/s	c)240 m/	's	d)5 m/s
the east direct	red 30 km in the ion during 2.5 h e of the average	,so .	_	then it covered 40 km in
	b)12.54 l peed of the car .			d)18.22 km/h
				d)27.42km/h
towards it at u the ball and ra		f 3 m/s , meanw ocity of 2 m/s tow	hile another pl	who was running layer was at 35 m from so the first player
b)before the sec	econd player by a econd player by a ond player by a eond player by at	atime of 0.55 s time of 0.83 s		
	ne average veloc			re x is measured In =2s to t=3s
a)50 m/s	b)30 m/s	c)26 m/s	d)10m/s	
the same direct equals	ction at velocity 2 	2v to cover a dis	tance 4d , so it	stace d , then it moves in ts total average velocity
a) v	<b>b)</b> 32 <b>v</b>	c) 2v	<b>d)</b> 53 <b>v</b>	
	ng in a straight r an average veloc			elocity v , then it moves
a) v	<b>b)</b> 32 <b>v</b>	c) 2v	<b>d)</b> 53 <b>v</b>	
distance at vel		and the rest of t	he distance w	r one third of the as covered at velocity of 
a)30 km/h	b)45 km/h	c)50 km/t	n d)6	55 km/h

			th a velocity 10 m/s then it moves average velocity of the body		
a)15 m/s	b)13 m/s	c)7.5 m/s	d)5 m/s		
•	_		10 m/s for a distance of 100 m then so the average velocity		
a)6.66 m/s	b)10 m/s	c)12.5 m/s	d)13.33 m/s		
10) a girl is running in a straight line with a constant velocity of 5 m/s from point A to point B, then she returns back in a straight line from point A to point B with a constant velocity 3 m/s so,  *the average speed during the whole journey equals					
11)the opposi	te graph describes	the motion of two	boys d <sub>(m)</sub>		
			A B x B		
	re moving in a unifo ollowing sentences	_	traight line .		
c)the velocitied) A precedes essay que	es of A and B are eq es of A and B are eq s B after passing po	jual at point x int x	speed		
•••••	•••••	•			

2)the opposite (displacement – time )graph describes the motion of a body in the straight line . Is the velocity of the body positive or negative or zero at :



a)t = 1s b)t = 2s c)t = 3s

# Lesson(2) Acceleration

#### 3-Acceleration:

We have discussed the concept of the variable velocity (magnitude, direction or both). Motion in which velocity changes with time is called the accelerated motion and the quantity that expresses the change of velocity per unit time is called acceleration (a). To investigate the concept of acceleration, study the following motion diagram that illustrates the readings of the speedometer of a car moving from rest and speeds up in a straight line.



#### Acceleration:

The change of the object velocity per unit time, or the rate of change of velocity. It is measured in  $(m/S^2)$  or  $(km/h^2)$ .

$$a = \frac{\Delta v}{\Delta t} = \frac{f_{inal\ velocity} - initial\ velocity}{F_{inal\ time} - initial\ time} = \frac{\Delta x}{\Delta t^2}$$

Note: You can convert the speedometer reading from km/h

into m/s by the relation:  

$$1 \text{km/h} = \frac{1000 \text{ m}}{60*60 \text{ sc}} = \frac{5}{18} \text{ m/s}$$

Example: Recording the data of an object moves with velocity (m/s) and time (s), we obtained by the table below:

Time (S)	0	1	2	3	4
Velocity (m/s)	0	5	10	15	20

It is obvious that the car speeds up at a constant rate where its velocity increases by (5m/s) every second. This value expresses the acceleration of motion that can be found by the relation:

$$a = \frac{change\ of\ the\ velocity}{change\ of\ time} = \frac{final\ velocity - initial\ velocity}{Final\ time - initial\ time} = \frac{20}{4} \text{5m/s}$$

## Types of acceleration:

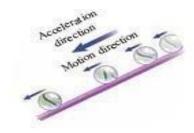
Objects may move at positive acceleration (increasing velocity), negative acceleration or deceleration (decreasing velocity) or zero acceleration (uniform velocity). These types can be identified by studying the following motion diagram that shows the motion of a small ball along frictionless planes of different inclination



As the ball climbs up the inclined plane, As the ball moves along the its velocity decreases with time and smooth horizontal plane, its acceleration is negative

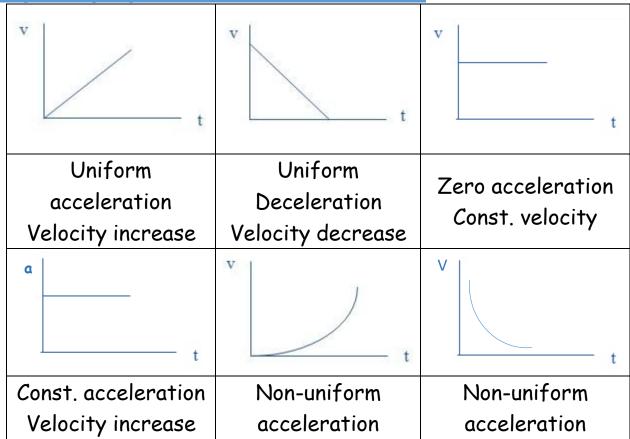


velocity does not change with time and acceleration equals zero



As the ball rolls down the inclined plane, its velocity increases with time and acceleration is positive

Graphically representation for acceleration:

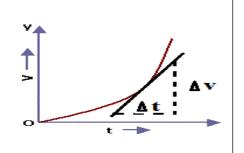


## **Types of acceleration:**

- 1. Uniform acceleration: It means that the rate of change invelocity is constant
- 2. Non uniform acceleration: It means that the rate change invelocity is variable
  - When  $\mathbf{v_f} > \mathbf{v_i}$  so it's a positive acceleration (+ ve)
  - When v<sub>i</sub> > v<sub>f</sub>so it's a negative acceleration (- ve)

It means also: The object moves with unequal amounts of velocity (velocity changes) with equal intervals of time.

Slope = 
$$\frac{\Delta v}{\Delta t}$$
 = acceleration (a)



## **Work sheet**

#### Choose the correct answer:

1) if a body starts its motion from rest and moves by acceleration a to reach a velocity

After time t, so its final velocity vf can be represented by the relation ......

- **b)** vf = at
- **c)**  $vf = 12 at^2$
- **d)**  $vf = \sqrt{at}$

2)if an object starts its motion from rest and speeds up at a constant rate till its velocity becomes 50 m/s during 10 s, this object moves at an acceleration of

**a)** $15 m/s^2$ 

- **b)**  $5 m/s^2$
- **c)**  $40 \ m/s^2$
- **d)**  $60 \, m/s^2$

3)a man starts its motion from rest with uniform acceleration 0f  $1 m/s^2$ , then his average velocity equals 1 m/s during ...... from starting his motion

- a)1 s
- b)2 s
- c)4 s

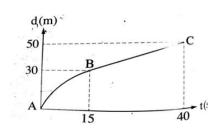
d)1/2 s

4)in positive acceleration ......

- a)initial velocity > final velocity
- b)initial velocity >final velocity
- c) initial velocity = final velocity
- d)velocity has variable direction

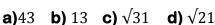
5)the opposite graph represents (d) and the time (t) for a body moves in a straight line, then the acceleration by which the body moves during the intervals AB and BC are .....

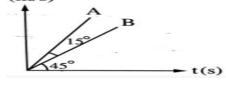
	AB	BC
а	Negative	Positive
b	Negative	zero
С	Positive	Positive
d	Positive	zero



6)the opposite graph shows the relation between velocity (v) and time (t) of two bodies A and B that start their motion from rest, so the ratio between the acceleration of body A and body B is ......

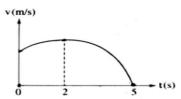






7)the opposite (velocity – time ) graph represents the motion of a car in a straight road , so which of the following sentences is correct?

- a)the car is static at t = 0
- b) the car returns to its starting point during 5 s



c) the dispalcement of the car increases from t = 0 to t = 5 s

d) the acceleration of the car is maximum at t = 2 s

8) which of the following senteces is correct ......

a)if the velocity of the body at a certain moment equals zero , the acceleration of the body at this moment must equal zero .

b)if the acceleration of the body equal zero, its velocity must be equal zero.

c) if the velocity of the body at a certain moment equals zero , the acceleration of the body at this moment may not equal zero .

d)the direction of the acceleration of a body is always in the direction of its velocity.

9)which case of the following cases is impossible to happen?.....

- a)a body is moving with velocity to the east and its acceleration is in the west direction
- b) a body is moving with velocity to the east and its acceleration is in the east direction
- c) a body is moving with variable velocity and costant acceleration
- d) a body is moving with costant velocity and variable acceleration

## essay questions

1)if a body starts its motion from rest and moves with uniform acceleration , where its average velocity during 2 sec from starting its motion is 3 m/s . calculate its average velocity during 5 sec from starting its motion

.....

2)a train moves with a uniform velocity of 40 m/s . it takes 6 seconds to pass a standing man , calculate the length of the train .

\_\_\_\_\_

In the previous chapter you have studied that the acceleration is the change in velocity per unit time. This acceleration may be uniform (constant) or varying or zero.

$$a = \frac{\Delta x}{\Delta t} \frac{\Delta x}{\Delta t^2}$$

Motion of an object at uniform acceleration has a special importance since it represents the motion of a number of objects in our experience. Examples may include those objects falling near the Earth's surface and projectiles.



Figure (13): falling of water from the top of a waterfall is at uniform acceleration



Figure (14): skating in air is a uniform acceleration

Assuming that an object moved in a straight line at uniform acceleration (a), and started motion from rest at initial velocity ( $v_i$ ) It reached a final velocity ( $v_f$ ) after an interval

(t) during which it was displaced through a displacement (d), We can describe such motion using three certain equations called equations of motion as follows:

## lesson (1)Equations of motion:-

# 1<sup>st</sup> equation of motion:

 $a = \frac{\Delta V}{t}$ 

$$a = \frac{Vf - Vi}{t}$$

$$At=Vf - Vi$$
  
 $V_f=v_i+at$ 

# 2<sup>nd</sup> equation of motion

(Displacement - time)

$$V_{av} = \frac{d}{t}$$

$$V_{va} = \frac{Vf + Vi}{2}$$

$$\frac{Vf + Vi}{2} = \frac{d}{t}$$

$$2d = (Vf + Vi) t$$
From 1st eq. (Vf = Vi + at)
$$2d = (Vi + at + Vi)t$$

$$2d = (2Vi + at) t$$

$$D = V_i t + \frac{1}{2} at^2$$

## 3<sup>rd</sup>eqyation of motion

(Displacement - velocity)

$$V_{av} = \frac{d}{t}$$

$$d = V_{av} \cdot t$$

$$\because V_{av} = \frac{Vf + Vi}{2}$$
From 1st eq.  $t = \frac{Vf - Vi}{a}$ 

$$d = \frac{Vf + Vi}{2} \times \frac{Vf - Vi}{a}$$
2ad =  $(Vf + Vi) (Vf - Vi)$ 
2ad =  $V_f^2 - V_i^2$ 

$$V_f^2 = V_i^2 + 2ad$$

The graphical representation of equations of motion ( $v_i=0$ )

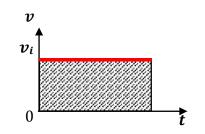
The 1st equation	The 2 <sup>nd</sup> equation	The $3^{rd}$ equation $2ad = v_f^2$	
$v_f$ = a $t$	$d = \left(\frac{1}{2} a t^2\right)$		
v t	d	V <sup>2</sup> d	
The slope = $\frac{v}{t}$ = a	The slope = $\frac{d}{t^2} = \frac{1}{2} a$	The slope = $\frac{v^2}{t}$ = 2a	

## If $(v_i \neq 0)$ the graphical representation will be:

The 1st equation	The 2 <sup>nd</sup> equation	The 3 <sup>rd</sup> equation
$v_f = v_i + at$	$d = \left(v_i t + \frac{1}{2} a t^2\right)$	$2ad = v_f^2 - v_i^2$
		$v_f^2$ $v_{i^2}$ $v_{i^2}$ $d$
The slope = $\frac{\Delta v}{\Delta t}$ = a	The slope = $\frac{\Delta d}{\Delta t^2} = \frac{1}{2} \alpha$	The slope = $\frac{\Delta v^2}{\Delta d}$ = 2a

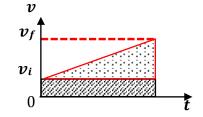
#### Deriving the second equation of motion graphically

In case of motion at **Uniform velocity** which is represented by straight line parallel to the time axis. Displacement= velocity \* time



Displacement= area under the graph  $d = v_i * t$  (1)

In case of motion at uniform acceleration we can divided the area below the curve into



- Area of rectangle =  $v_i * t$
- Area of triangle =  $\frac{1}{2}$  \* Base \* hight =  $\frac{1}{2}$  \* t \*  $(v_f - v_i)$

But 
$$(v_f - v_i) = a t$$

So area of triangle = 
$$\frac{1}{2}$$
 a  $t^2$  (2)

By adding (1) + (2) we will find 
$$d = (v_i t + \frac{1}{2} a t^2)$$

## Some important special cases:

The general	a body start	a body stops	moves with
formula	from rest	$(v_f = 0)$	uniform
	$(v_i = 0)$		velocity
			(a =0)
$v_f = v_i + at$	$v_f$ = a $t$	$-v_i$ = a $t$	$v_f = v_i$
$d = (v_i t + \frac{1}{2} a t^2)$	$d = \left(\frac{1}{2} a t^2\right)$	$d = (v_i t + \frac{1}{2} a t^2)$	$d = v_i t$
$2ad = v_f^2 - v_i^2$	$2ad = v_f^2$	$2ad = -v_i^2$	$v_f = v_i$

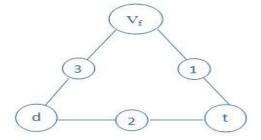
## Guidelines may help to solve the problems:

- 1) If the object moves at a uniform velocity, it's acceleration= zero Because(the change in velocity  $\Delta v = 0$ )
- 2) When the object starts the motion from the rest, itsinitial velocity  $v_i$  = zero.
- 3) If the driver applies the break till the car stops its final velocity  $v_f$  = zero.
- 4) If the object moves in a straight line with uniform acceleration, it's average velocity is given from relation

- 5) If  $(v_f > v_i)$  speed increases it means: acceleration is **positive** (if velocity is positive).
- 6) If  $(v_i > v_f)$  speed decreases it means: acceleration is **negative** (if velocity is positive).
- 7) If the velocity and acceleration have **the same direction**then they have **the same sign (accelerating motion)** if both where in (+ve) direction or in (-ve) direction.
- 8) If the velocity and acceleration have **the opposite direction** then they have the **opposite sign** (**decelerating**).
- 9) When? Means find the time (t).
- 10) Where? Means find the displacement (d).

## **Key of problem**:

This triangle is used to solve equations of motion where the number indicates number of equation to solve the problem.



## Work sheet

## **Choose the correct answer:**

landing on a s	straight runwa 50 m/s when to rates uniforml	ay of an air po ouching the s y by a rate of	ort , if you know that its surface of the run way $2 m/s^2$				
a)5 s	b)10 s	c)12.5 s	d)25 s				
2)a radar monitors the motion of the car that moves on a straight road with uniform acceleration of -4 $m/s^2$ , it finds that the velocity of the car was 13 m/s at 10:05:00 am, then its velcoity at *10:04:59 am equals							
a)17 m/s	b)9m/s	c)7m/s	d)5m/s				
*10:05:01 am	equals		••••••				
a) 17 m/s	b)9m/s	c)7m/s	d)5m/s				
3)a train moves at a straight line with an acceleration of 2 $m/s^2$ that has an opposite direction to its motion . then the time required to change its velocity from 72 km/h to 13 km/h equals							
a)6.2 s	b)8.2 s	c)11.8 s	d)29.5 s				
4)if an object starts its motion from rest in astraight line with uniform acceleration and takes time (t) which is numerically equal to the magnitude of its acceleration (a) to reach a final velocity of 16 m/s, so the magnitude of the acceleration							
<b>a)2</b> <i>m/s</i> <sup>2</sup>	<b>b)4</b> m/s <sup>2</sup>	<b>c)8</b> <i>m/s</i> <sup>2</sup>	<b>d)16</b> <i>m/s</i> <sup>2</sup>				

acceleration sec is 1.5 m/	rts its motion in astraight less, so its insta after 30 sec	ine . if the a ntaneous v from startir	average verelocity is ng its moti	elocity durin ion	ıg 8	
a)15.4 m/s	D)12.5 II	1/S C)11	.25 m/s	d)9.25 m/s		
acceleration starts its mo	acement of a is given by the tion with access $0m/s$ , then its .	ne relation deleration a=	$d=v_it+12a$ $\mathbf{i}=2\ m/s^2\mathbf{w}$	$at^2$ and the behicles and the highest the highest part and the highest part $at^2$	_	
a)100 m	b)200 m	c):	300 m	d)400 m		
8 sec, then i	ve in straight it movesin the of 4 $m/s^2$ for equals	same dire 6 sec , so t	ction with	a uniform		
a)128 m	b)80 m	C	)68 m	d)56 m		
8) two bodies start their motion from rest and move in astraight line with uniform accleration to cover a distance (d) . if the time taken by the first body to cover this distance is double the time taken by the second body , then the ratio between the acceleration of the first body and the acceleration of the second body is						
<b>a)</b> 12	<b>b)</b> 11	<b>c)</b> 14	<b>d)</b> 116			
9)a train of length 100 m enters a straight tunnel of length 1 km with a velocity of 4 m/s . if the train is moving by acceleration of $0.5\ m/s^2$ , then the required time for the entire train to leave the tunnel is						

a)550 s	b)58.81 s	c)20.31 s	d)20 s				
10)a tiger started running when it saw a deer runing at uniform velocity of 2m/s at 15 m far from it . if the tiger ran at acceleration of 2 $m/s^2$ , then the tiger catch the deer after : *passing a time of from starting the motion							
a)5 s	b)4 s	c)2.5 s	d)1 s				
*covering a dis	tance of	•••••					
a)25 m	b)15 m	c)10 m	d)5 m				
uniform accele 7.5 m/s through	ist started motion ration of 1.5 $m/s^2$ n a displacement of b)18.75 m	. so its velocit of	y has reached				
12)the final velocity of a body moving with uniform acceleration is given by the relation : $v_f = \sqrt{v_i^2 + 2ad}$ . if the initial velocity of the body is 6 m/s and it moves by an acceleration of 4 $m/s^2$ , then its velocity is after covering a displacement of 8m							
a)5 m/s	b)10 m/s	c)15 m/s	d)20 m/s				
13)a car is moving with velocity of 56 km/h and the minimum distance that would be taken by the car to stop is 12 m . if the car moves with velociity of 113 km/h , then the minimum distance would be taken by the car to stop is $\frac{1}{2}$							
( Assuming that a)97.7 m	t the acceleration b)49.2 m	is constant in c)48.9 m	both cases ) d)24.4 m				

when it cov	vers distance	rmaly from res (d) , so the vel n starting its n	ocity of t	he car when it
a) v	<b>b)</b> $\sqrt{2}$ <b>v</b>		) 2 v	d) 4 v
acceleration displacement	on , if its avera ent of 20 m , th	on from rest ange velocity is nen its averages	10 m/s w e velocity	hen it covers a / during 8 sec
a) 2 m/s	b)40 m/s	c) 10 m/s	d)80 r	n/s
essay ques	stions :			
acceleration acceleration	of 2 $m/s^2$ to cov	er a distance of	100 m , th 200 m . ca	en it moves with
•••••		• • • • • • • • • • • • • • • • • • • •		
•••••	• • • • • • • • • • • • • • • • • • • •	•••••	• • • • • • • • • • • • • • • • • • • •	
•••••		• • • • • • • • • • • • • • • • • • • •		
•••••	• • • • • • • • • • • • • • • • • • • •	•••••	• • • • • • • • • • • • •	•
••••••	• • • • • • • • • • • • • • • • • • • •	••••		

## Lesson 2

# Applications of motion with uniform acceleration (Free fall – Vertical projectiles)

## 1) Free fall:

If we drop a book and a sheet of paper at the same instant from the same height, which of them reach the ground first? But, when the sheet of paper is placed adjacent to the book topside and allowed to fall, what would you observe? Explain your observation.

When an object falls to ground, its motion is affected by two forces:

- 1) Gravitation pull of earth (their weight).
- 2) The air resistance due to collisions between the object and air molecules.

The impact of this resistance is greater on the velocity of falling of light objects than that of heavier objects. Note that no air resistance affected the sheet of paper when it was placed adjacent to the topside of the book during falling.



Conclusion: To simplify this issue, we are going to study the fall of objects under the effect of their weights, only neglecting the effect of air resistance. This motion is called free fall. It is worthy to mention that at the absence of air resistance, all objects fall to the ground at the same acceleration.

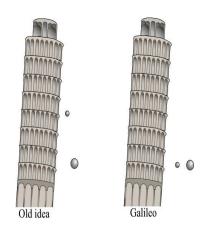
#### Notes:

- 1) if the objects fall under the effect of their weights only and acquire a uniform acceleration that acts to increase the speed of falling gradually till it reach its maximum value when touching the ground this acceleration called free fallacceleration which is uniform acceleration.
- 2) The free fall acceleration varies slightly from one position to another on the Earth's surface **because** the Earth's surface is not completely spherical but it's elliptical, where its equatorial diameter is bigger than its polar diameter, so the free fall acceleration varies depending on the distance from the Earth's center.
- 3) The average value of free fall acceleration equals (9.8 m/s $^2$ ) for the simplicity it can be considered (10 m/s $^2$ )

## **Distinguished scientists:**

Galileo proved that falling objects of different masses reach the ground at the same time, when air resistance is neglected.

By dropping two objects of different masses down Tower of Pisa. This experiment put an end for Aristotle thoughts that implied that heavier objects would reach the ground first.



## Free fall acceleration (q):

It is the uniform acceleration of objects that fall freely. This acceleration equals  $(9.8 \text{ m/s}^2)$  and means that the **object's** velocity when falling freely increases by (9.8 m/s) every second.

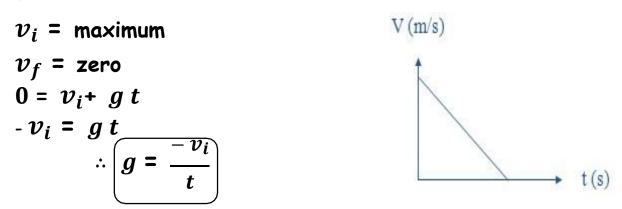
When an object falls under the effect of gravity we can apply the motion equations:

$$v_f = v_i + gt$$
  $d = (v_i t + \frac{1}{2} g t^2)$   $2gd = v_f^2 - v_i^2$ 

## 1) When an object falls freely (from up to down):

$$v_i$$
 = zero  $v_f$  = max. before touching the ground  $v_f = 0 + g t$   $g = \frac{v_f}{t}$ 

## 2) When an object is projected vertically (upwards):



g:is (-ve) because the body moves against the earth's gravity

#### **Example 1:**

A stone fell from the roof of a building. If the stone passed by a man standing in a balcony 5 m high above the ground (2 seconds later) (consider  $g = 10 \text{ m/s}^2$ )

- a) The building height
- b) The stone velocity at the moment of passing by a man.

$$v_i = 0$$

Solution: 
$$v_i = 0$$
 g = 10 m/s  $t = 2s$ 

$$t = 29$$

$$d_2 = 5m$$

a) The height of the building (h) = the distance from roof tobalcony  $(d_2)$  + the distance from balcony to ground  $(d_1)$ 

$$d_2 = (t_1 + \frac{1}{2}gt^2) = 0 + () * (10) * (2)^2 = 20 \text{ m}$$

The height of the building (h) =  $d_1 + d_2 = 20 + 5 = 25$  m

b) The stone velocity when it passes in front of the man

$$v_f = v_i + g t$$
 = 0 + (10) \* (2) = 20 m/s

## Example 2:

An apple has fallen freely from a tree and reached the ground  $(q = 10 \text{ m/s}^2)$ after 1 sec. Find:

- Its velocity at the moment of hitting the ground.
- b) The average velocity of the apple during falling.
- c) The height from which it fell

Solution:  $v_i = 0$ 

$$t = 1s$$

a) Velocity at reaching the ground  $v_f$ 

$$v_f = v_i + g t$$
 = 0 + (10) \* (1) = 10 m/s

b) (Average velocity) 
$$v = \frac{v_f + v_i}{2} = \frac{10 + 0}{2} = 5 \text{ m/s}$$

c) The height from which the apple fell

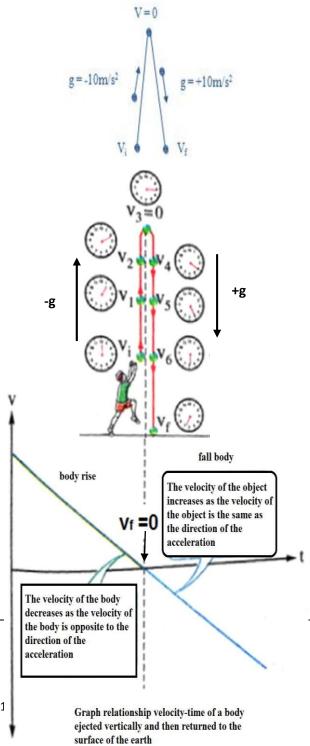
$$d = (t_1 + \frac{1}{2}gt^2) = 0 + *(10) *(1)^2 = 5 \text{ m}$$

## **Projectiles:** there's two types of projectiles

- a) Vertical projectiles b) Two-dimensional projectiles

## a) Vertical projectiles:

- a) When an object projected vertically upwards, it starts at initial velocity  $(v_i)$  which doesn't equal zero and moves with uniform acceleration (-ve) ≈  $-10 \text{ m/s}^2$ .
- **b)** The velocity of the object decreases gradually as the object gets higher and reaches zero at the maximumheight.
- c) The direction of velocity changes when the object returns back to the ground under the effect of Earth's gravity that makes the object accelerate (+ve)  $\approx (10 \text{m/s}^2).$
- **d)** The velocity of the object when it's projected up = (-ve) its velocity at the same height when it falling down.
- **E)** The time of rising to the maximum height = the time of falling to the same level of projection.
- **F)** The total flight time = The time of rising + the time of falling.



Example 3: An object projected vertically upwards at initial velocity 98 m/s find:  $(q = 9.8 \text{ m/s}^2)$ 

- a) The maximum height reached by the object.
- b) The time taken to reach that height

**Solution:** 
$$v_i = 98$$
  $v_f = 0$   $g = -9.8$  m/s  $t_1 = ??$   $d_1 = ??$ 

a) 
$$2gd = v_f^2 - v_i^2$$

$$2 * (-9.8) * d = 0 - (98)^2$$

$$2*(-9.8)*d=0-(98)^2$$
 d=  $\frac{-(98)}{2*(-9.8)}$  = 490 m

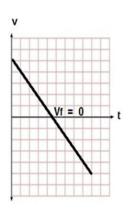
b) 
$$v_f = v_i + g t$$

$$0 = 98 - 9.8 (t)$$

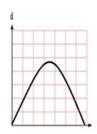
$$0 = 98 - 9.8 (t)$$
 So  $89 = 9.8 (t)$   $t = 10 sec$ 

$$t = 10 sec$$

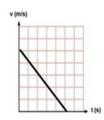
## Note: Important graph relationships



An object was ejected vertically and then returned to the surface of the earth

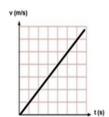


An object was ejected vertically and then returned to the surface of the earth



vertically projected body upwards slope =-q

$$V_f = V_i + gt$$



A body in a free fall slope = g

$$V_f = V_i + gt$$

0

		W	<mark>'ork sheet</mark>			
<b>Choose the</b>	correct answe	er:				
			ds to reach the	maxi	imum height (h) after 3 s	,
_	lue of (h) is				<b>3</b>	
			d)60 m			
•			0		me fall freely together fr e following statements is	
a)the heavi	er body reach	es the ground	d first .			
b)the lighte	r body reache	s the ground	first .			
_	er body accel	_				
	h the ground					
-						
3)an object	falls freely . g	iven that (g=	=10 <i>m/s</i> <sup>2</sup> ), its ve	locity	y 3 seconds later become	S
••••	•••••			·		
a)29.4 m/s	b)98 m/s	c)19.6 ı	m/s d)9.8	3 m/s		
m high abo	ve the ground respect	, then the tin	ne taken by ea	ch bo	me moment from a point ody to reach the ground i	
reach the si	urface , then t	_	h above the mo		surface . if it takes 2 s to vity equals	)
	at the body mo		c)0.8 m/s <sup>2</sup>			
the well . ho		nds will pass	to hear the sou		at 122.5 m from the edg f the stone hitting the wa	

7)a man drops astone from the top of building and when the stone covers  $10\,\mathrm{m}$  the man drops another stone , if the height of the tower is  $100\,\mathrm{m}$  , then the time difference between the dropping of the two stones is .......

a) 1/2 s

a)4.64 s

b)  $\sqrt{2} s$ 

b)5s

c) 2 s

c)5.36 s

d)  $2\sqrt{2} s$ 

d)5.72 s

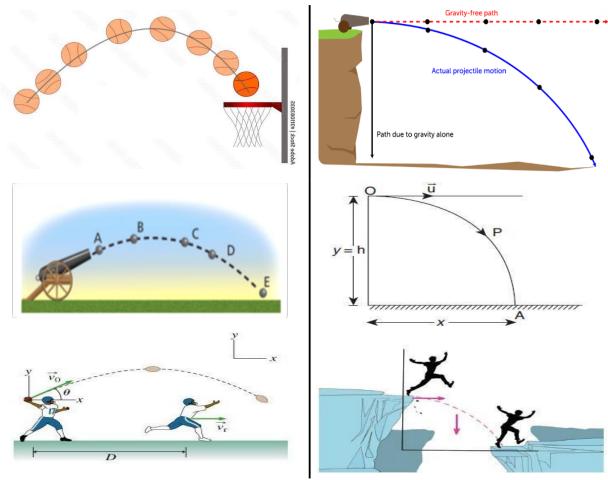
of its motion	is v m/s, then	•	_	a distance of 1m from the start e start of its motion is
a) $v^2$	m/a b) 2v	c) $v^2/2$	d) $\sqrt{2} v$	
of the buildir		, so it covers t	_	d) , then it reaches the middle of the building during time
		c) 0.33 t	<b>d</b> ) <b>0.</b>	41 t
level with the	e same initial v	elocity , where	one of them i	tically upwards from the same s metallic and the other is ensity of the wood , then
b)the metallic)the wooden	c ball reaches t	level of projecti the level of proj he level of proj answer	ection first	ne instant
1.25 m, so th		of this player in		r in the basketball game was
12)a body is j	projected verti	cally upwards	to reach max	imum height of 80 m, then
a)39.6 m/s b)	of the projection of the projection of the project	on is n/s d)14 m/s v to return to th		ojection is
a)2.85 s b)4.0	04 s c)5.71 s d)8	3.08 s		
(g=10m/s2)		<b>v</b> -		velocity 98 m/s , then :
a)147 m/s		n/s	c)49 m/s	d)24.5 m/s
	m height reach 0 m c)414 m d)	ned by the body )397 m	· · · · · · · · · · · · · · · · · · ·	••••••
*the total tim	ne taken by the			tion till it returns to the point
a)10 s		9 s		d)20 s

14)an object is p	rojected vertical	ly upwards with	n initial velocity of 60 m/s , the	en:
(g=10m/s2)				
*the time taken	by the object to 1	reach avelocity	of 20 m/s is	•••
a)8 s b)4 s c)2 s d	d)0.25 s			
*the height of th	e object when it	reaches a veloci	ty of 20 m/s is	
a)320 m	b) 200 m	c)160 m	d)80 m	
15)a stone is thre	own vertically do	ownwards at vel	ocity of 96 m/s into a well to 1	each the
bottom after 3 s	, then the depth	of the well is	( $g$ =10 $m$	's2)
a)376.2 m	h) 332 1 m	c)243 2 m	d)199 8 m	•

## <u>b)</u> (lesson3) Projectiles when projected at an angle (Motion in two dimensions):

We have studied the motion of objects at uniform acceleration in a straight line either in a horizontal, inclined or a vertical plane. At the moment, we are going to study objects motion when projected at an angle to the horizontal under the effect of gravity.

A projectile such as a ball or a cannonball is launched with an initial velocity  $v_i$  at an angle  $\theta$  with the horizontal, it moves in a curved line like shown in the figures.



We can resolve velocity in Two dimensions Horizontal (x) And vertical (y) as shown in the figur

Horizontally the body moves at a constant speed Because the horizontal acceleration = zero

 $v_{2x}$ 

 $v_{3x}$ 

• The horizontal velocity can be determined from:

 $v_{1x}$ 

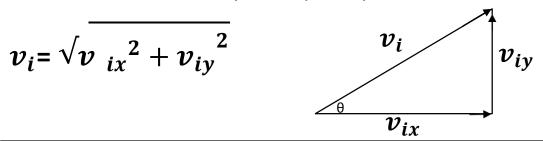
$$v_{ix} = v_i \cos \theta$$

 $v_{0x}$ 

The vertical velocity can be determined from:

$$v_{iv} = v_i \sin \theta$$

• You can calculate velocity of body at any instant from:



**Note:**  $v_{ix}$  is constant so  $v_{ix} = v_{fx}$ 

Horizontal velocity is uniform because  $a_x = 0$ 

## 1) Finding the time of reaching maximum height (t):

 $v_{fy}$  =  $v_{iy}$  +  $\mathsf{g}t$  , but at maximum height  $v_{fy}$  =0

$$\therefore -v_{iy} = \mathbf{g}t \qquad \text{so} \qquad \boxed{t = \frac{-2\mathbf{g}}{\mathbf{g}}}$$

## 2) Finding the flight time (T):

It's the time taken by the body from the initial point of motion till it returns back to the plane of projection, its double the time of reaching the maximum height.

$$T = 2 t = \frac{-2 v_{iy}}{g}$$

# 3) Finding the maximum height reached by the projectiles (h):

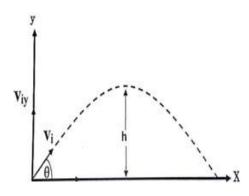
When the body reaches the maximum height , the velocity in the vertical direction vanished ( $v_{fy}$ =0)

$$2gd = v_{fy}^2 - v_{iy}^2$$

d is the distance we can state it (h) because we describing the height

$$2gh = 0 - v_{iy}^{2}$$

$$h = \frac{-v_{iy}^{2}}{2g}$$



# 4) Finding the horizontal range (the horizontal distance reached by the projectiles) (R):

: The time of maximum horizontal range = Flight time = T

To find distance we can use 2<sup>nd</sup> equation

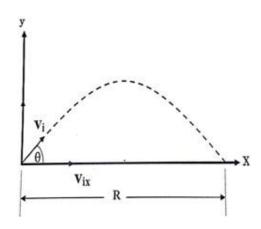
$$d = v_{ix} t + \frac{1}{2} a t^2$$

in x-direction  $a_x = 0$  and (d = R) in the second equation of motion so it will be:

$$R = v_{ix} * T$$

but 
$$T=2t$$

and 
$$t = \frac{-v_{iy}}{g}$$
 by substitutin



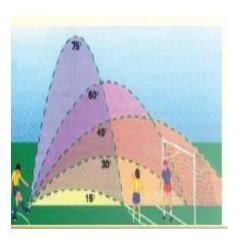
$$R = v_{ix} * \frac{-2v_{iy}}{g}$$

#### **Notes**:

1)The projectile reaches its maximum horizontal range (R)

When projected at an angle of 45° and the maximum height in this case equals  $(\frac{\kappa}{-})$ .

2) The horizontal range of two objects is the same if they projected at complementary angles (their sum is 90°) and at the same initial velocity.



Example: A motorcycle is launched at a speed of 15 m/s in a direction that makes  $30^{\circ}$  with the horizontal. (g = 10 m/s<sup>2</sup>)

- a) What is the maximum height reached by motorcycle?
- b) How long does it fly?
- C) What is the maximum horizontal range a bike can reach?

$$v_{i}$$
= 15 m/s

$$\theta = 30^{\circ}$$

$$v_i$$
= 15 m/s  $\theta$  = 30° g = 10 m/s<sup>2</sup> Firstly I

have to calculate  $oldsymbol{v}_{oldsymbol{i}oldsymbol{x}}$ 

and 
$$v_{iy}$$

$$v_{ix} = v_i \cos \theta = 15 \cos 30 = 12.99 \text{ m/s}$$

$$v_{iv} = v_i$$
 sin  $\theta$ 

$$v_{iv} = v_i \sin \theta = 15 \sin 30 = 7.5 \text{ m/s}$$

a) The maximum height (h) = 
$$\frac{-viy^2}{2g} = \frac{-(7.5)^2}{2(-10)} = 2.8 \text{m}$$

b) The time of the flight (T) = 
$$\frac{-2 v_{iy}}{g} = \frac{-2 (7.5)}{-10} = 1.5 \text{m}$$

c) The horizontal range (R)

= 
$$v_{ix}$$
 \* T = 12.99 \*1.5

=19.48m

## **Work sheet**

## **Choose the correct answer**

,	orojectile which is vel after time T , t 	•		
<b>a)</b> 1/2 T	<b>b)</b> <i>T</i>	<b>c)</b> 2 <i>T</i>	<b>d)</b> <i>T</i> /2	
•	al displacement reach ted at the same initia	•		
a)80° and 60	)° b)40° and 50°	c)80 $^{\circ}$ and 20 $^{\circ}$	d)80° and 30°	
,	s projected upwards and some some some some some some some some	_		
a)5 m <sup>′</sup>	b)10 m c)15	m d)20	m	
to the horizont *the maximum	ected from the earth's al , then height reached by th b)5 m c)15 m	e ball is	-	an angle of 60°
surface is	horizontal range read s b)38.5 m c)41.3	-	when it returns to tl	he earth's
surface after 4 *the initial velo	orojected at an angle s , then : city by which the obj b)40 m/s c)35 m/s	ect is projected		
*the horizontal	component of the ob	ject's velocity a	t the moment of the	projection is
a)30√3m/s	<b>b)20</b> √3 m/s <b>c)10</b> √3	m/s d)5 √3m/s		
	height reached by th )20 m c)5 m	e object is d)1.25 m		
horizontal, so	t is placed on the gro the initial velocity tha om the cannon is	at is required for	r firing the projectile	s to hit a target
a)150 m/s	b)100 m/s c)75 m/s	d)50 m/s		

## **Chapter (3): Force and motion**

Previously we have described motion by studying the conceptsof velocity and acceleration without getting into the reasons beyond. In this chapter we are going to discuss the existence of acceleration due to the impact of a force. This leads us to Newton's laws of motion that are considered as basic laws inphysics.

#### Force:

Is an external influence that affects the object to change its state or direction of motion (from rest to motion or vice versa.

Force is measured by the spring balance in Newton (N). Examples:



- 1-Your muscle strength helps you move bodies.
- **2-**The Force of the car engine helps the car to start motion.3-Brakes force acts to stop the car.

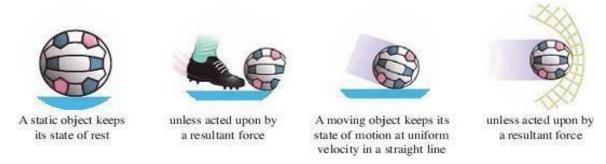
## 1) Newton's first law:

A body keeps its state of (rest) or (motion at a uniform velocity in a straight line) unless acted upon by a resultantforce that changes its state.

The mathematical formula of the law is

$$\Sigma F = 0$$

The symbol (  $\Sigma$  ) pronounced sigma or summation it means the resultant force.



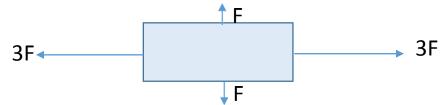
The term  $\Sigma F$  is the resultant force that may equal zero when the forces acting on an object may cancel the effect of each other.

Applying Newton's First Law, we can draw a conclusion that when the resultant force = 0, acceleration = 0, and no change happens in object velocity either being static or dynamic. Also, a resultant force is needed to move a static object or to stop a moving one. No need for a resultant force to move objects at uniform velocity in a straight line.

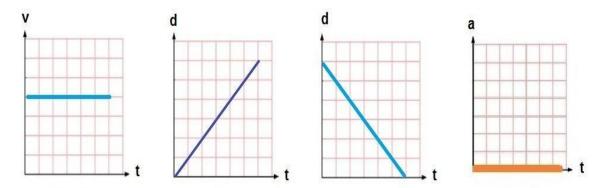
Give reasons .....?!!

1- Two or more forces act on an object but its state didn'tchange?

Because the Resultant force on this body = zero



#### Graphic relationships that apply to Newton's first law:



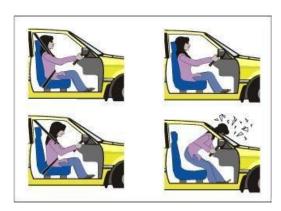
In all of the previous cases, the net force on the moving body = zero because objects are moving at a constant velocity, acceleration (a) = zero.

• Newton's first law is known as the law of Inertia.Inertia:

It's the tendency of an object to keep either its state of rest or state of motion at its original velocity uniformly in a straight line. This means that objects resist changing its static or dynamic state.

Or "it is the property of objects to resist the change of its static or dynamic state".

In the shown figure when a woman driving a car with a certain velocity and suddenly used the brakes so the car will stop but her body still in the motion state.



#### **SO** we can say

- 1- Newton's first law known as the law of inertia **because** the object **can't change** its state of rest or motion in straight line**by itself**.
- 2- Seatbelt should be fastened on driving to stop inertia during sudden stop and protect passengers from being hurt.

#### Technological applications:

When being away from the Earth's gravity, a space rocket does not need to consume fuel to keep moving because inertia keeps it moving at uniform velocity in a straight line.

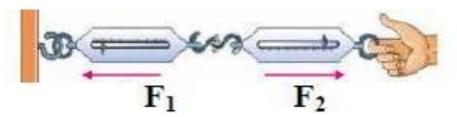


- 2) Newton's second law will be studied in the second term
- 3) Newton's Third law:

When an object acts on another object by a force, the second object reacts with an equal force on the first object in a direction opposite to that of action."

**I.e.** For every action there is a reaction **equal in magnitude** and **opposite in direction**.

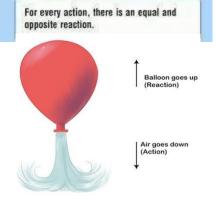
The mathematical formula that expresses the law: F1 = -F2



#### **Examples**:

- 1- When a man jumps from a boat to the reef (action), The boat shifts backwards (reaction).
- 2- When a bullet is fired (action) the rifle recoils backwards (reaction).so the soldier should mount the rifle back firmly to his shoulder.
- 3- When blowing up a balloon and leaving it free, the trapped air pushes out the open end (action), causing the balloon to move upwards (reaction)





#### **Notes:**

- **1-** No single force can exist in the universe **because** action andreaction are paired forces; originate and vanished together.
- 2- Although they are equal, it's not a must that action and reaction are at equilibrium **because** the two forces acts on different bodies and equilibrium condition happens when thetwo forces act on the same body.
- **3- Action and reaction** are of the same **type**; if the action is gravitational force the reaction is a gravitational force, as well.

#### Note:

For two forces to be at **equilibrium**, they must be **equal**, **opposite**, **having one line of action** and **act on the samebody**.

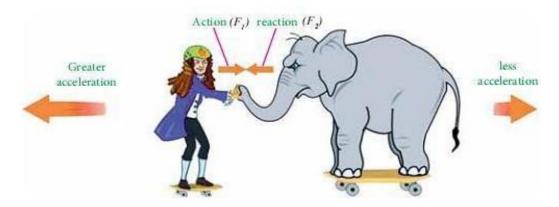
#### **Technological application**

Launching a rocket is based on Newton's third law of motion.

A huge amount of burning gases rush down the rocket to generate a reaction pushing the rocket upwards.

#### Example1:

#### Study the following figure, then answer the question below



- 1. What is the relation between the force acting on the elephant and that on the man?
- 2. Why the action on the elephant and reaction on the man are **not** at equilibrium?

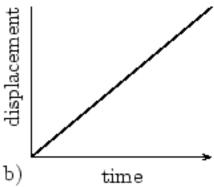
## Solution:

- 1. The force acting on the elephant = the force acting on theman. F1= -F2
- 2. For two forces to be at equilibrium, they must be equal, opposite, having one line of action and act on the same body. All these conditions except the last one may be applied on action and reaction; since the action acts on the elephant andthe reaction is on the man.

## **Work sheet**

#### Choose the correct answer:

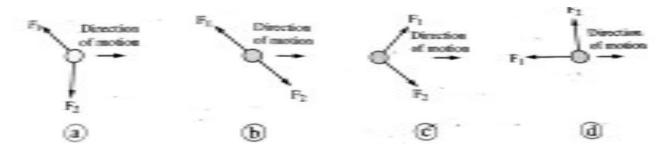
1)the opposite graph represents the relation between the displacement and time of a body of mass 10 kg that moves in straight line, so the



acting resulting force on the body equal .....

a)30 N b) 300 N c) 3 N d)0

2)which of the following figures represents a body that moves with a uniform velocity (v) under the effect of two equal forces in magnitude  $F_1$  and  $F_2$ ?



3)in the opposite figure, there are three spring balances that are in equilibrium state, if the reading of each of the first and the second balance is  $100~\rm N$ , so the reading of the third balance is .....



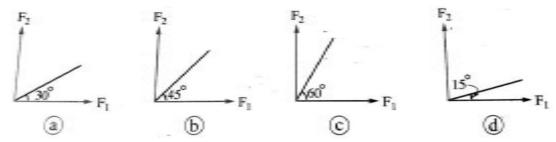
a)0 b)25 N c)50 N d)100 N

4)when blowing up a ballon and leaving it free , the ballon moves

- a)in the direction of the air rush
- b)in a direction right to the direction of the air rush
- c)in the opposite direction of the air rush
- d)in a direction left ti the direction of the air rush

5)which of the following graph represenst the relation between the magnitude of the reaction force F2

And the magnitude of the action F1 when drawn by the same drawing scale?



6)if an astronaut who is floating in the space projection a small object in the same direction of (a) as an opposite figure,



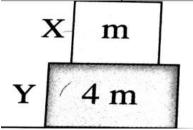
the astronaut will .....

- a)move in the direction of (a)
- b) move in the direction of (b)
- c) move in the direction of (c)
- d)not move

7)if a body (x) acts on another body (y) by a force of  $9\ N$ , then the reaction force of a body (y) on body (x) equals

.....

- a) 1N b) -9 N c)0 d) 9 N
- 8) the opposite figure shows body (x) that is placed above body (y) and both of them are in rest. if body (x) acts on body (y) by a force of F downward, then body (y) acts on body (x) by a force ......



essay questions:  1)can a body be in a state of equilibrium when it is affected by a single force ?? explain .	
2)explain why car manufacturing companies have added safety belts to each car.	
3)mention the action nd reaction forces in each of the following cases : a)a man moves in the street	
b)a catches the football c)a window is closed due to the wind blowing	
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b)a catches the football c)a window is closed due to the wind blowing a)	
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